



Investigation of Thermodynamical parameters of $Zn_xMg_{(1-x)}$ TS Single Crystals

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Abstract: A wide variety of novel inorganic, organic and semi organic non-linear optical materials are being developed in recent years. For the transmission of data, in many devices photons are used instead of electrons and the development in nonlinear optical crystals aids this application. In this aspect, in the present work tailor-made semi-organic NLO crystals of $Zn_xMg_{(1-x)}$ TS were grown by slow evaporation techniques for various values of x (x = 0 to 1). The density of the grown crystals was determined by conventional flotation technique and composition was estimated from the measured density. The thermodynamical parameters like melting point, thermal stability, thermal activation energy, frequency factor, entropy, enthalpy and Gibb's free energy were determined by using Broido Method, Coats and Redfern Method and Horowitz and Metzger Method from the TG/DSC curves recorded in the temperature range 30 to 1010°C. The thermal activation energy, frequency factor, entropy and enthalpy were determined to vary non-linearly with bulk composition, and also observed that the thermodynamical parameters obey Horowitz and Metzger method.

Key Words: ZMTS mixed crystals, Density, Thermal activation energy, Entropy, Enthalpy, Gibb's free energy.

1. Introduction

Semi-organic materials gains prominence in the non-linear optics for real time applications[1]. The organic ligand and inorganic host was subjected to ionic bonding, results in novel materials with good optical nonlinear property [2]. The TG/DTA was found to be a proficient one for the estimation of thermal behaviour and also describes the decomposition levels of the materials [3]. In earlier study N. Bhuvaneshwari Arvind et al [4] reported that Tris-Thiourea Magnesium Zinc Sulphate crystal was thermally stable up to 248.75°C. A. Darlin Mary et al [5] studied the thermogravimetric analysis of ZTS and MTS mixed crystals. The magnesium when mixed with ZTS, the melting point of ZTS was found to be increased and then decreased slightly. The melting point of MTS was found to be 181.40°C. The thermal stability of ZTS was found to decrease with the addition of different concentration of magnesium and observed a no phase transition till the materials melt. V.S. Kumar and R.S.

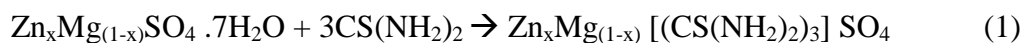
Sundararajan [6] reported that Tris-Thiourea Zinc Magnesium Sulphate crystal was thermally stable up to 265°C. I.B.Patel [7] observed that the thermal stability of ZTS was 202.73°C. Using the Broido relation they calculate the activation energy, frequency factor, entropy, enthalpy and Gibbs energy. The activation energy, frequency factor for the temperature range 202.73°C -310°C was found to be -1.4237×10^{-23} kJ and 28.38 min^{-1} respectively. G.Pasupathi and P.Philominathan [8] have reported that the melting point of MTS was 153°C. S.Gunasekaran et al [9] have studied the thermal properties of UMTS, BMTS and TMTS. They reported that the melting point of UMTS, BMTS and TMTS are 232°C, 231°C and 236°C respectively. S.Alfaify et al [10] added Mg^{2+} and M.Selvapandiyani et al [11] added $MgSO_4$ to ZTS. They all reported that thermal stability and melting point of doped ZTS was greater than that of pure ZTS, and also pointed out that increase in thermal stability and melting point may be due to the incorporation of dopant atom.

In the present research work mixed crystals of $Zn_xMg_{(1-x)}TS$ were grown by slow evaporation technique. The density of the crystals was determined by conventional flotation technique and bulk composition was also determined from the density values. Thermodynamical parameters were evaluated from TG/DSC curves using Broido method, Coats and Redfern method and Horowitz and Metzger method. Section 2 describes the experimental details and the results are highlighted in section 3

2. Experimental Details

The ZMTS salts were synthesized by the stoichiometric mixing of Zinc Sulphate heptahydrate and Magnesium Sulphate heptahydrate with Thiourea in the molar ratio 1:3. The compounds are dissolved in deionized water, followed by stirring using a magnetic stirrer and finally the mixture was heated at 50°C.

The chemical reaction involved in this process is as follows



where, $x = 0$ to 1 in steps of 0.1

The slow evaporation technique was employed in this research work for the growing of Single crystals of ZMTS. Totally eleven crystals were grown (9 mixed and 2 end member crystals). The density of the crystals were determined by conventional flotation technique using bromoform (2.894 g/cc) and ethanol (0.78 g/cc) as higher and lower density liquids respectively. The bulk compositions of the mixed crystals were estimated from the density of the grown crystals. The crystalline properties of a sample can be estimated from its melting behavior via thermal analysis. Thermal analysis gains prominence industrial sector, it depicts the change in the physical property of material with respect to temperature [12, 13 and 14]. The thermal characterization of the grown crystals was studied using TG/DSC curves recorded in the temperature range 30 to 1010°C using STA 449F3 Jupiter Instrument at NETZSCH Technologies India Pvt. Ltd, Chennai. The thermodynamical parameters like melting point, thermal stability, thermal activation energy, frequency factor, entropy, enthalpy and Gibb's free energy were determined from the TG/DSC curves.

Thermal activation energy is the minimum amount of energy needed to initiate thermal reaction or it can also be defined as the energy that is required in a chemical system for the chemical reaction to take place. There is much literature works describing the different techniques for the estimation of thermal activation energy [15-22]. In this research work, the thermal activation energy and kinetic parameters were estimated by using Broido method, Coats and Redfern method and Horowitz and Metzger method.

In the Broido model the activation energy at each stage of decomposition (E_a) and the frequency factor (A) was evaluated from the Arrhenius relation

$$\ln \ln \left(\frac{1}{y} \right) = \frac{-E_a}{RT} + \text{Constant} \quad (2)$$

$$\text{Where } y = \frac{w_t - w_\infty}{w_o - w_\infty}$$

y is the fraction of the number of molecules not yet decomposed, w_t is the weight of the material, w_o is the initial weight of the material and w_∞ is the weight of the residue.

To determine the activation energy, plot a curve between $\ln(\ln(\frac{1}{y}))$ versus $1/T$. From the slope of line of best fit, the activation energy (E_a) was determined and the intercept gives the frequency factor (A).

The expression for the estimation of activation was put forward by Coats and Redfern, the order of the reaction is a vital parameter.

For first-order reaction when $n = 1$ the equation is as follows

$$\log_{10} \left(\frac{-\log(1-\alpha)}{T^2} \right) = \left[\log_{10} \left\{ \left(\frac{AR}{\alpha E_a} \right) \left(1 - \frac{2RT}{E_a} \right) \right\} - \left(\frac{E_a}{2.303RT} \right) \right] \quad (3)$$

$$\text{Where } \alpha = \frac{w_o - w_t}{w_o - w_f}$$

w_o is the initial weight, w_t is the weight at time and w_f is the final weight of the material. A plot of $\log_{10}[-\log(1-\alpha)/T^2]$ versus $1/T$ will result in a straight line having slope ($E_a/2.303R$) from which activation energy (E_a) was calculated and the intercept gives the frequency factor (A).

The activation energy was estimated using the integral equation of Horowitz and Metzger. The equation used for the estimation of energy of activation (E_a) is as follows

$$\ln \ln \left(\frac{w_o}{w_t} \right) = \frac{\theta E_a}{RT^2} \quad (4)$$

where, $\theta = (T - T_s)$, the difference between the maximum temperature and the temperature at particular weight loss, w_o is the initial weight, w_t is the weight at any time t , T_s is the maximum temperature and T is the temperature at particular weight loss. A plot of $\ln \ln(w_o/w_t)$ versus θ gives a straight line. From the slope the activation energy can be calculated.

Entropy is the energy that is distributed or dispersed among the various motions of molecules of the crystal. The entropy (ΔS) can be calculated using the relation [23].

$$\Delta S = 2.303 \times R \times \log_{10} \left[\frac{Ah}{kT} \right] \quad (5)$$

where, R is the universal gas constant, A is the frequency factor, h is the Planck's constant, k is the Boltzmann constant and T is the melting point.

Enthalpy is the heat that evolved or absorbed in the reaction. The Enthalpy (ΔH) was calculated using the equation [24]

$$\Delta H = E_a - RT \quad (6)$$

where, E_a is the Energy of activation.

Gibb's free energy is associated with a chemical reaction that can be used to do work. It can be determined from entropy and enthalpy by using the relation

$$\Delta G = \Delta H - T\Delta S \quad (7)$$

3. Results and Discussion

The photograph of all the grown crystals are shown in figure1. The morphology of the crystals grown in the present study were diamond shape of 1mm thickness and they are opaque and white in colour.



Top : ZTS, MTS, $Zn_{0.1}Mg_{0.9}TS$, $Zn_{0.2}Mg_{0.8}TS$

Middle : $Zn_{0.3}Mg_{0.7}TS$, $Zn_{0.4}Mg_{0.6}TS$,

$Zn_{0.5}Mg_{0.5}TS$, $Zn_{0.6}Mg_{0.4}TS$

Bottom : $Zn_{0.7}Mg_{0.3}TS$, $Zn_{0.8}Mg_{0.2}TS$, $Zn_{0.9}Mg_{0.1}TS$

Fig. 1: Photograph of all the grown crystals

The measured density and the bulk composition estimated from the density values are given in Table.1.

Table 1: Density and Estimated bulk composition of all the grown crystals

Sample	Density (g/cc)	Estimated bulk Composition
ZTS	1.7317 [1.942] [26]	-
MTS	1.6038 [1.6087] [27]	-
$Zn_{0.1}Mg_{0.9}TS$	1.6149	$Zn_{0.0868}Mg_{0.9132}TS$
$Zn_{0.2}Mg_{0.8}TS$	1.6318	$Zn_{0.2189}Mg_{0.7811}TS$
$Zn_{0.3}Mg_{0.7}TS$	1.6401	$Zn_{0.2838}Mg_{0.7162}TS$
$Zn_{0.4}Mg_{0.6}TS$	1.6520	$Zn_{0.3769}Mg_{0.6231}TS$
$Zn_{0.5}Mg_{0.5}TS$	1.6654	$Zn_{0.4816}Mg_{0.5184}TS$

$Zn_{0.6}Mg_{0.4}TS$	1.6829	$Zn_{0.6185}Mg_{0.3815}TS$
$Zn_{0.7}Mg_{0.3}TS$	1.6972	$Zn_{0.7303}Mg_{0.2697}TS$
$Zn_{0.8}Mg_{0.2}TS$	1.7120	$Zn_{0.8460}Mg_{0.1540}TS$
$Zn_{0.9}Mg_{0.1}TS$	1.7226	$Zn_{0.9289}Mg_{0.0711}TS$

The density value reported earlier for ZTS and MTS single crystal are given in square brackets. It is found that the density of the mixed crystals shows linear variation with the composition of zinc. As the composition of the zinc increases the density of the mixed crystals also found to be increased. The composition estimated for the mixed crystals from the density values well agreed with the actual composition taken.

Inference from the TG/DSC curve: TG/DSC curve for the mixed crystal $Zn_{0.5}Mg_{0.5}TS$ crystal is shown in figure 2 for illustration. The crystals grown in the present research study was found to be thermally stable from 180°C to 195°C. The grown crystals do not contain the water molecule because there is no weight loss around 100°C.

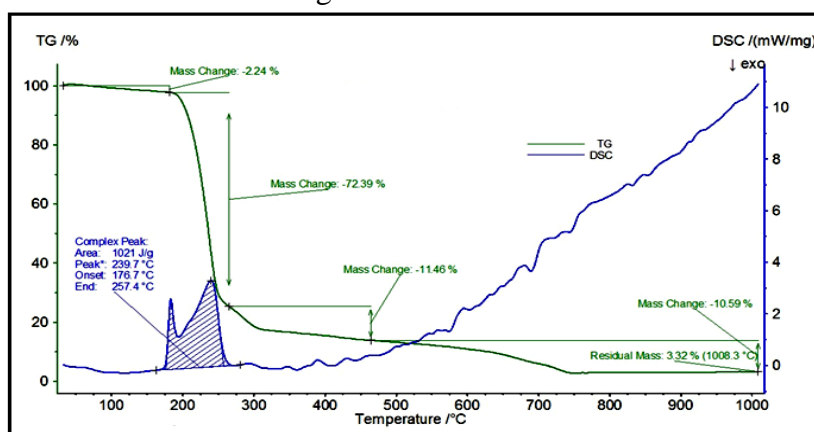


Fig. 2: TG/DSC curve of $Zn_{0.5}Mg_{0.5}TS$ crystal

The graph drawn between $\ln \ln \left(\frac{1}{y}\right)$ Vs $1/T$ for the mixed crystal $Zn_{0.7}Mg_{0.3}TS$ is shown in the figure3.

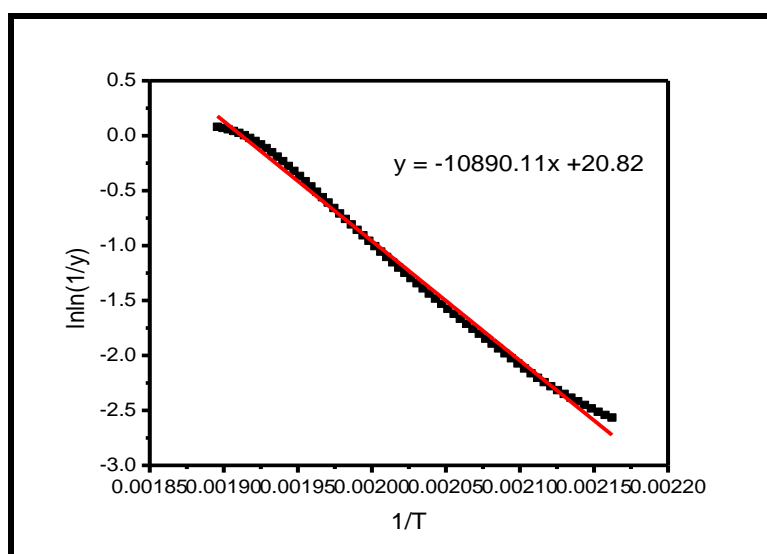


Fig. 3: Variation of $\ln \ln(1/y)$ with $1/T$ for $Zn_{0.7}Mg_{0.3}TS$ crystal

The curve drawn between $\log_{10} [-\log(1-\alpha)/T^2]$ versus $1/T$ for the mixed crystal $Zn_{0.3}Mg_{0.7}TS$ is shown in the figure 4.

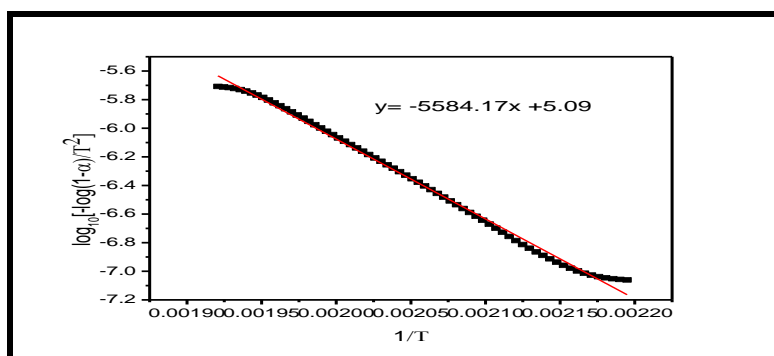


Fig. 4: Variation of $\log_{10} [-\log(1-\alpha)/T^2]$ with $1/T$ for $Zn_{0.3}Mg_{0.7}TS$ crystal

The graph drawn between $\ln \ln(w_o)/(w_t)$ versus θ for the mixed crystal $Zn_{0.8}Mg_{0.2}TS$ is shown in the figure 5 for illustration.

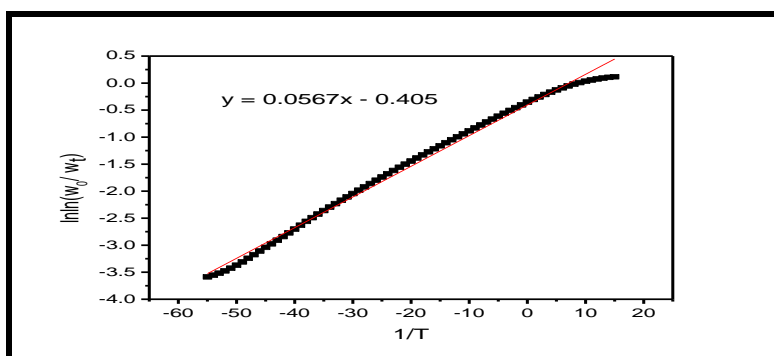


Fig. 5: Variation of $\ln \ln(W_o/W_t) 1/T$ for $Zn_{0.8}Mg_{0.2}TS$ crystal

The results in graph reveal that, transitions follow a straight line and obey the Arrhenius behaviour. Negative slope was observed in the transitions on the heating scan due to the heat absorption. The endothermic peak shift towards the lower range temperature values with respect to the decrease in ramp rate [25]. In the case of Horowitz and Metzger method positive slope is obtained. The melting point of the ZTS and MTS crystals agreed with the values reported earlier. The melting point of the mixed crystals shows non-linear variation with bulk composition. The variation of activation energy with composition for the three models is shown in figure 6.

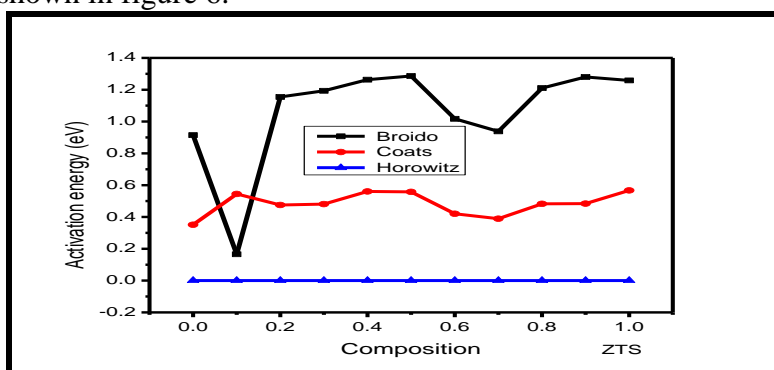


Fig. 6: Variation of Activation energy (eV) with composition for the three methods

The melting point and thermal stability are given in the Table2.

Table 2: Melting point and Thermal Stability for all the grown crystals

Sample	Melting Point (K)	Thermal stability (°C)
ZTS	495.3 [504][28]	191.66
MTS	508.5 [454.40][5]	189.15
$Zn_{0.1}Mg_{0.9}TS$	531.7	193.31
$Zn_{0.2}Mg_{0.8}TS$	526.9	189.15
$Zn_{0.3}Mg_{0.7}TS$	509.4	185.00
$Zn_{0.4}Mg_{0.6}TS$	512.3	185.00
$Zn_{0.5}Mg_{0.5}TS$	512.7	189.15
$Zn_{0.6}Mg_{0.4}TS$	515.1	189.15
$Zn_{0.7}Mg_{0.3}TS$	510.9	181.09
$Zn_{0.8}Mg_{0.2}TS$	515.1	185.00
$Zn_{0.9}Mg_{0.1}TS$	509.3	181.19

The activation energy determined is low and it also varies non-linearly with bulk composition. The low activation energy indicates the autocatalytic effect of the metal ion on the thermal decomposition of the crystal [29]. The variation of entropy and frequency factor with composition for the three models is shown in figures 7 and 8 respectively.

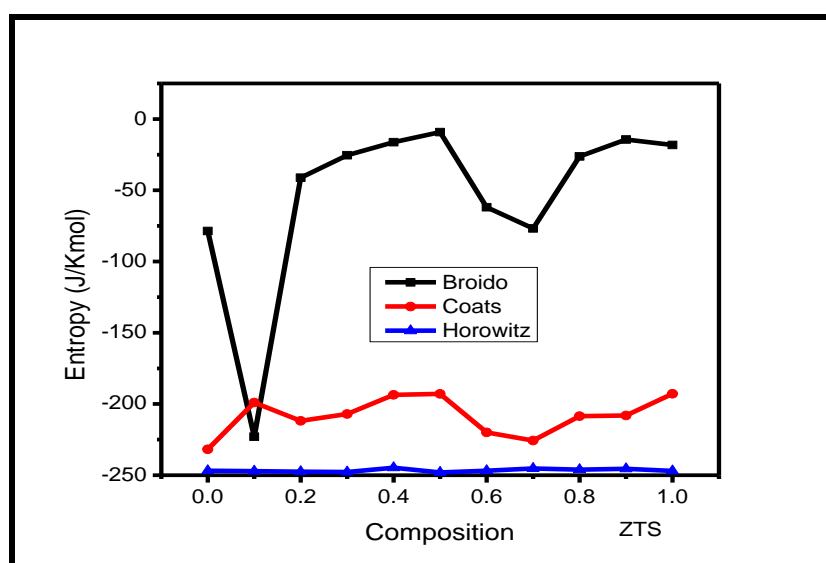


Fig.7: Variation of Entropy (J/K mol) with composition for the three methods

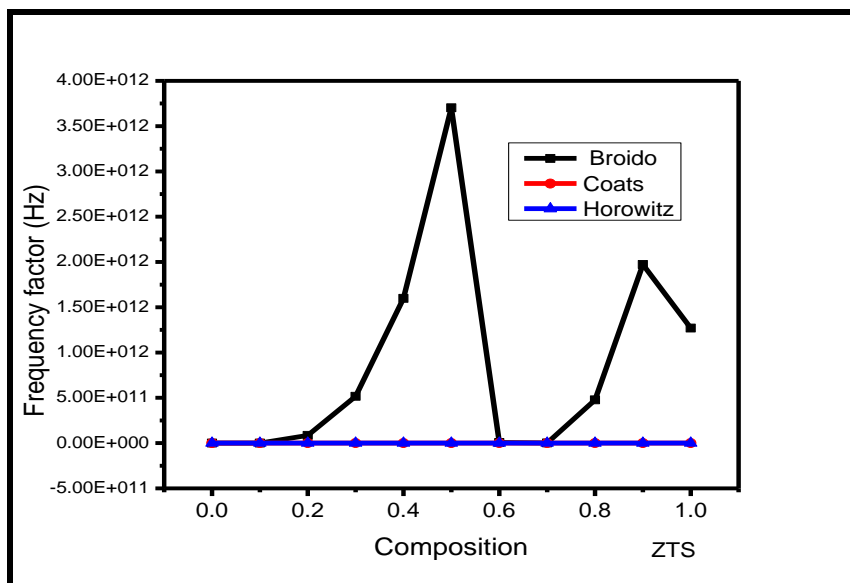


Fig. 8: Variation of Frequency factor (Hz) with composition for the three methods

The entropy of all the mixed crystals show a non-linear variation with bulk composition and the value is negative. The activated complex was found to be more ordered, since the entropy value is negative. The high value of A indicates the fast nature of reaction. The polarization of bonds and fast nature of reaction accounts for the ordered nature of the activated complex [23].

The variation of enthalpy with composition for the three models is shown in figure 9.

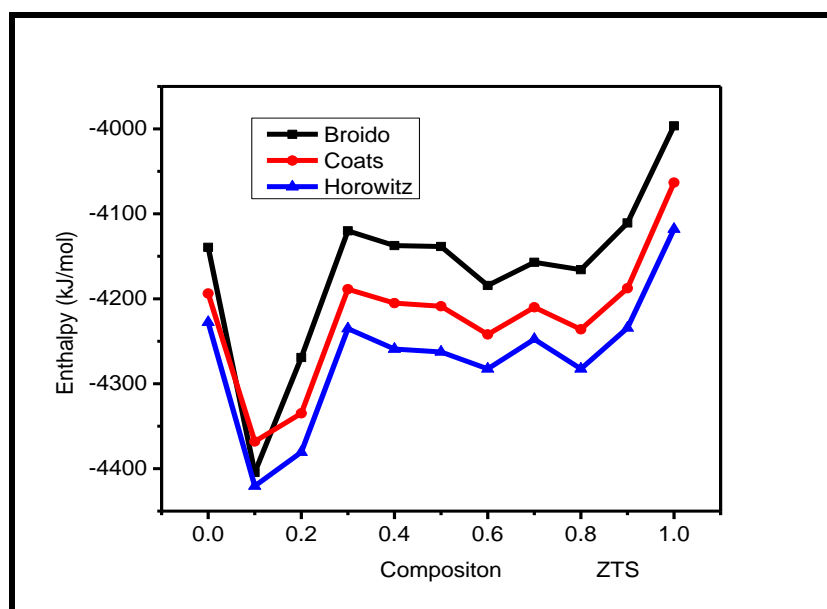


Fig. 9: Variation of Enthalpy (kJ/mol) with composition for the three methods

The enthalpy of reaction determined for the mixed crystals are negative and almost same. The negative sign indicates that the reaction is exothermic. The variation of Gibb's free energy with composition for the three models is shown in figure10 respectively.

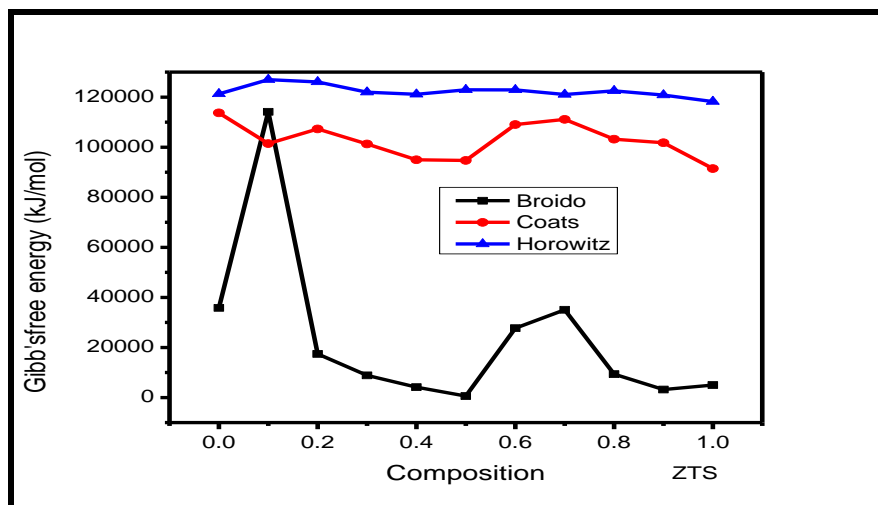


Fig. 10: Variation of Gibb's free energy (kJ/mol) with composition for the three methods

Gibbs energy determines the useful work delivered by a system and is a vital characteristic of a system. It determines, whether a state change is spontaneous or not. The ΔG value may be positive or negative and it is an indication of nature of the reaction; spontaneous or non-spontaneous. The negative value of ΔG represents the spontaneous nature of the reaction and positive value of ΔG represents the non-spontaneous nature of the reaction [30]. Gibb's free energy determined in the present investigation is almost constant for all the mixed crystals using the Coats and Horowitz methods. The positive value of Gibb's energy shows that the reaction is non-spontaneous towards the products and spontaneous towards the reactants. Thermodynamical parameters like thermal activation energy, frequency factor, entropy and enthalpy determined vary non-linearly with bulk composition. From the figures 6, 7, 8 and 10 the parameter varies linearly with composition determined from the Horowitz and Metzger method when compared to the other two methods. So we concluded that the Horowitz and Metzger method is suitable for this current system.

4. Conclusion

Thermodynamic properties of $Zn_xMg_{(1-x)}TS$ Single Crystals was investigated in this research work. The activation energy was determined by three methods; Broido, Coats and Redfern and Horowitz and Metzger methods. The activation energy varies non-linearly with bulk composition. The entropy of all the mixed crystals shows a non-linear variation with bulk composition and the value is negative. The enthalpy change is observed to be negative. The negative sign indicates that the reaction is exothermic. The positive value of Gibb's energy shows that the reaction is non-spontaneous towards the products and spontaneous towards the reactants. The Horowitz and Metzger method was found to be proficient in the estimation of activation energy.

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